Superconducting nano-mechanical diamond resonators

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ABSTRACT
In this work we present the fabrication and characterization of superconducting nano-mechanical resonators made from nanocrystalline boron doped diamond (BDD). The oscillators can be driven and read out in their superconducting state and show quality factors as high as 40,000 at a resonance frequency of around 10 MHz. Mechanical damping is studied for magnetic fields up to 3 T where the resonators still show superconducting properties. Due to their simple fabrication procedure, the devices can easily be coupled to other superconducting circuits and their performance is comparable with state-of-the-art technology.

1. Introduction
Nano-mechanical resonators allow to explore a variety of physical phenomena. From a technological point of view, they can be used for ultra-sensitive mass \cite{1-3}, force \cite{4-6}, charge \cite{7,8} and displacement detection. On the more fundamental side, they offer fascinating perspectives for studying macroscopic quantum systems. Significant progress has been made in the last few years by cooling a nano-mechanical resonator into its ground state \cite{9-12}. Couplings between nano-mechanical resonators and superconducting circuits have been realized and even the creation of entanglement with these macroscopic oscillators seems in reach \cite{13}. In order to exploit such a system in quantum information technology, nano-mechanical systems will have to be coupled to other quantum systems such as light \cite{14} or superconducting circuits \cite{9,15-20} and new materials to improve the coupling for such hybrid systems are of importance. In this respect diamond is an extremely attractive material. Despite the fact that diamond has exceptional mechanical properties \cite{21-24}, it has a relatively high refractive index which allows to couple it to light. In addition when doped with boron, it can be rendered superconducting with remarkable electrical properties and makes it a promising material for fully integrated hybrid nano-mechanical systems.

In this article we present the fabrication and characterization of nano-mechanical resonators built out of superconducting diamond. We demonstrate a simple top down process to fabricate these resonators by common electron beam lithography and hence offer a simple way to be implemented into superconducting circuits. We compare their performance to state-of-the-art resonators and investigate the limits of their...
superconductivity. Quality factors around 40,000 at around 10 MHz resonance frequency are demonstrated and it is shown that it is possible to directly read out a superconducting resonator at a magnetic field as high as 3 T.

2. Fabrication

The nano-mechanical resonators have been fabricated from a superconducting nanocrystalline diamond film, grown on a silicon wafer with a 500 nm thick SiO$_2$ layer. To be able to grow diamond on the Si/SiO$_2$ surface, small diamond particles of a diameter smaller than 6 nm are seeded onto the silica substrate with the highest possible density [25]. A subsequent microwave plasma chemical-vapor deposition (CVD) allows to grow and control various properties of the film. It is possible to vary the grain sizes from few nanometers to few microns by controlling the methane concentration. Furthermore one can add a variety of dopants to drastically change some of the key properties of pure diamond. While adding boron gas during the CVD process one can turn the elsewise insulating diamond film metallic and above a critical concentration even superconducting [26,27]. A detailed description of this growth process can be found in reference [25].

The nano-mechanical structures have been defined using standard electron beam lithography. First, a 70 nm thick nickel etch mask, which defines the sample geometry has been evaporated on top of the diamond film, which has then been followed by anisotropic oxygen plasma etching [28]. The sample is cooled to 10 °C while being exposed to the oxygen plasma for approximately 8 min. The anisotropy of the etching process leads to straight walls that broaden less than 5 nm after 300 nm of etching. After this process, the nickel mask is removed by dipping the sample in a FeCl$_3$ solution. To provide good ohmic contacts, a tri-layer consisting of titanium, platinum and gold has been evaporated followed by annealing at 750 °C. The structures have been suspended by etching the sacrificial SiO$_2$ layer using HF vapor at 50 °C and atmospheric pressure for about 10 min. Diamond itself is inert to this chemical etching process. Due to the strong mechanical stiffness, tri-critical point drying has not been necessary even for structures with lengths up to 30 μm. Fig. 1 displays a suspended diamond structure that has been fabricated by this method. We have also fabricated superconducting diamond resonators that were covered with a 50 nm thick gold layer in order to test the samples at temperatures above the superconducting transition temperature and at currents above the superconducting critical current. This allows for easy detection of the resonance conditions. For this purpose a slightly modified technique was used. After the e-beam process, a metallic bilayer of 50 nm gold and 50 nm of nickel was deposited instead of 70 nm nickel as in the previous case. This bilayer acts as a mask for the etching process. The nickel layer was subsequently removed using FeCl$_3$, which does not attack the gold layer. Finally the combination of diamond and gold layer was exposed to HF gas for suspension. The etch rate of gold in HF at the temperatures used is negligible [29].

In the following, we mainly discuss the results of two resonators, one with a geometry of 30 μm × 480 nm (length × width) and one with 25 μm × 350 nm with a 50 nm gold layer on the top, referred to as sample A and sample B, respectively. The thickness of the diamond film was estimated to 300 nm using an optical profilometer.

3. Measurements

The low temperature characterization of the nano-mechanical beams was done using the magneto-motive detection scheme [30]. The radio frequency signal from a network analyzer (Rohde – Schwarz ZVL-13) was fed into a coaxial line at the top of a 3He cryostat with a base temperature of 500 mK. The signal was delivered to the sample through two attenuation stages: 20 dB at 4.2 K and 20 dB at the 1.2 K stage. An ac-current flowing through the sample exposed to a perpendicular external magnetic field $B$ induces a Lorentz force that actuates the beam and leads to a displacement of the nano-mechanical beam in plane to the diamond film. On resonance, the beam dissipates energy changing its impedance and resulting in a dip in the transmission signal. The transmitted signal is amplified at 4.2 K with a gain of approximately 50 dB (Caltech CILTF1 SN120) and fed into the input port of the network analyzer. The same electrical setup also allows for characterization of the superconducting properties of the nano-mechanical resonators.

To verify whether our resonators show superconductivity, we first measured the superconducting transition as a function of the input power and temperature at a frequency of approximately 9 MHz close to the expected resonance frequency. The input power can in principle be directly converted into a current using a perfectly 50 Ω adapted circuit model. However, since this approach neglects the change of sample impedance when sweeping through the resonance as well as contact resistances, it is more convenient to directly plot the input power instead of the bias current. Nevertheless, the calculated critical currents are of the order of

![Fig. 1 – Scanning electron micro-graph of a diamond resonator. The dimensions of the resonator are 480 nm × 300 nm (width × thickness). Different resonators with different lengths ranging from 5 to 30 μm have been fabricated.](image)
few µA, similar to what has been measured with DC measurements of similar nanostructures made from BDD [31,32]. The transmission signal of sample B is plotted in Fig. 2. One can clearly identify a constant transmission plateau at low input powers (temperature) at lower input powers (temperatures) at higher magnetic fields. The transition is shifted to lower input powers (temperatures) at higher magnetic fields. (A colour version of this figure can be viewed online.)

From the total transmission drop we can calculate the approximate normal state resistance values to around 300 Ω for sample B. We have obtained similar data for sample A and a normal state resistance close to 2.5 kΩ (not displayed). The difference in resistance is due to the presence of the gold layer on top of sample A. At higher magnetic fields, the superconducting transition is shifted to lower input powers and to lower temperatures and a residual resistance appears which can be associated to the increase of quasiparticles in the superconductor. We obtained a superconducting transition temperature of approximately 2.5 K at zero magnetic field in agreement with measurements on non-suspended diamond samples [28,31,32].

We now turn to the mechanical properties of the diamond nano-mechanical resonator. By applying a perpendicular magnetic field and sweeping the RF frequency of the bias, the resonators can be actuated and their characteristics can be extracted. In Fig. 3 we show a typical transmission signal at resonance obtained from sample A. The resonance frequency of resonator A and B are 9.39226 MHz and 8.77142 MHz, respectively. Using

\[ f_{\text{res}} = \frac{1}{2\pi} \sqrt{\frac{Y_L}{\rho w^2}} \]  

with \( \chi = 4.73 \) being a numerical factor for the beam’s first flexural mode [34], \( I_y \) being its moment of Inertia, \( w \) its width, \( l \) its length and \( \rho \) the density of diamond, we can calculate the Young’s modulus to 950 and 810 GPa, respectively. The difference between the Young’s moduli of sample A and B is simply due to the additional metal layer of the latter. In addition, the fact that the Young’s modulus is as high as the one observed for undoped nanocrystalline diamond [35,36] shows that the boron doping does not degrade the mechanical properties.

From the transmission measurement we can also extract the loaded quality factor \( Q \), which describes the rate of energy loss, compared to the energy stored in the resonator. For sample A and B we find \( Q = 40,000 \) and \( Q = 30,000 \), respectively. From these measurements we conclude that the Young’s modulus as well as the quality factor of sample B is lower due to enhanced losses caused by the gold layer on top of the structure. The effect of the gold layer is to modify the mechanical properties in terms of surface stress, additional mass, additional elasticity and damping. Such effects have been studied in detail in the literature [37–39].

A side effect of the magneto-motive detection technique is the circulation of eddy currents inside the structure, which leads to an additional magnetic field that is opposed to the applied external magnetic field. This results in an additive force that is opposed to the beam movement and leads to another damping term \( Q_e \) that adds linearly to the intrinsic mechanical damping.

\[ \frac{1}{Q} = \frac{1}{Q_{\text{mech}}} + \frac{1}{Q_e} \]  

The eddy current damping [40] scales with \( B^2 \) and adds to the inverse of the intrinsic quality factor which is independent of the magnetic field and only depends on the intrinsic mechanical losses. Fig. 4 shows the corresponding magnetic damping for sample A from which we extract the intrinsic unloaded quality factor \( Q_{\text{mech}} = 41,000 \) at zero magnetic field. This mechanical quality factor is limited by the surface roughness of the diamond and more importantly by clamping losses due to the doubly-clamped beam design. The isotropic etching of the sacrificial SiO₂ layer leads to an undercut of the
anchor pads of the NEMS. The more surface undercut the more dissipation is possible in the vibrating surroundings of the resonator’s clamps, the higher the losses. Possible solutions to increase this quality factor would be to use the so-called free-free beam design [40], to reduce the surface losses by smoothing the surface with mechanical or chemical polishing before nanofabrication [41] and to remove the undercut by means of a focused ion beam technique. Nevertheless, the observed quality factors are comparable with state-of-the-art resonators [23,42,43]. A commonly used value for comparison is the product of frequency and quality factor, $fQ$, for which we obtain $3.85 \times 10^{11}$.

To convince oneself that the measured resonance is of mechanical nature and not of some electrical resonance, we plot the signal amplitude as a function of magnetic field in Fig. 5. Following [44] we can fit our curves using

$$S_{12} = -20\beta \log \frac{2Z_0}{\sqrt{aB^2 + 2Z_0}}$$

(3)

where $aB^2 = Z_c = \frac{n^2}{z_{sh}}$ is the resonators impedance, $\beta$ adjusts the amplitude of the signal, $Z_0$ is the line impedance and $\zeta$ is a constant of order unity, depending on the mode shape [44].

The transmission signal of the resonator A shows a finite residual resistance at finite magnetic field as depicted in Fig. 2. This resistance can be seen as the real part of an external embedding impedance in series with the nano-mechanical oscillator. Assuming that this embedding impedance changes slowly over the resonance width, which is justified in our case as the damping is low, we find that the loaded resonance frequency shifts according to [44]

$$f_l = f_0 \sqrt{1 + \Theta \left(B - B_c\right)Z_c \frac{\Re(Z_{ext})}{|Z_{ext}|^2}}$$

(4)

where $f_0$ is the unshifted frequency at zero embedding impedance. Assuming that the second term in Eq. (4) is zero below a critical field $B_c$ for the superconducting resonator we can fit our data of the resonance frequency shift as shown in Fig. 6. From the fit we extract the critical field to $B_c = 0.996$ T which is consistent with the onset of the residual resistance of sample A (not displayed).

4. Conclusion

We have demonstrated that nano-mechanical resonators made from boron doped diamond show superconducting properties up to magnetic fields of 3 T. These resonators show high quality factors as high as 40,000 at a resonance frequency of around 10 MHz. The simple fabrication process of superconducting diamond resonators allows for easy implementation into fully superconducting diamond circuits such as micro-cavities or superconducting quantum interference devices. Due to its remarkable mechanical, electrical as well as optical properties we conclude that nano-mechanical resonators made from boron doped diamond offer an extremely attractive system in the growing field of quantum optomechanics.

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